Operations Research

Objectives: This course is an introduction to operations research. Topics are chosen from convex optimization, analysis of variance, categorical data analysis, and nonparametric statistics.

Prerequisites: Linear Algebra, Analysis I and II, Probability and statistics

Syllabus

- **1.** Convex functions on real line. Properties of smoothness. Conjugate convex functions. Remarkable inequalities.
- **2.** Convex sets in linear spaces. Affine sets and convex sets. Separation theorems. Extremal points. The orthogonal projection.
- **3. Convex functions on normed vector spaces.** Continuity. Support. Subdifferential. Rademacher's theorem. Classes of differentiable convex functions.
- **4.** Elements of optimization theory. Maxima and minima. Minimax theorems. Applications to game theory. Linear programming. The simplex method. Convex programming.
- 5. Statistical thinking and data analysis.

Bibliography

- 1. S. P. Boyd and L. Vandenberghe, *Convex optimization*, Cambridge Univ. Press, 2004.
- 2. J. Céa, Optimisation. Théorie et Algorithmes, Dunod, Paris, 1971.
- 3. C. P. Niculescu and L.-E. Persson, *Convex Functions and their Applications. A Contemporary Approach*, Springer-Verlag, 2006.
- 4. A. Wayne Roberts and Dale Varberg, *Convex Functions*, Academic Press, 1973.

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